

## Supplemental material to the article

### “Magnetic properties of $\text{Li}_2\text{RuO}_3$ as studied by the NMR and the LDA+DMFT calculations”

#### 1. Details of crystal growth

To prepare the polycrystalline samples, appropriate quantities of  $\text{Li}_2\text{CO}_3$  and  $\text{RuO}_2$  (both Alfa Aesar, at least 99.99 % purity) were mixed using an agate mortar and pestle and dried in a furnace at  $600^\circ\text{C}$  in air overnight. The powder was then pressed into 10 mm diameter pellets and heated at  $900^\circ\text{C}$  for 15 h followed by sintering in an alumina crucible at  $1000^\circ\text{C}$  for four days, with intermediate grinding. A 10 mol % excess of  $\text{Li}_2\text{CO}_3$  was used to compensate for evaporation of Li. All heating was done in a muffle furnace. The sample purity was monitored using a Rigaku MiniFlex benchtop X-Ray diffractometer employing Cu-K $\alpha$  radiation. Our bulk resistivity and differential scanning calorimetry measurements show clear signs of the phase transition at around 560 K, indicative of the high quality of our samples.

#### 2. NMR details

$^7\text{Li}$  NMR measurements were carried out over the temperature range (100–700) K on the AVANCE III 500WB BRUKER spectrometer in magnetic field  $H_0 = 11.74\text{ T}$ . The static broad spectra of  $^7\text{Li}$  (the nuclear spin  $I = 3/2$ ; quadrupole moment  $^7Q = -0.04 \times 10^{-24}\text{ cm}^2$ ) were obtained by means of the spin echo signals with subsequent Fourier transformation of the acquired signals. The magic angle spinning (MAS) NMR spectra of  $^7\text{Li}$  were obtained using a 3.2 mm rotor with a spinning speed of about 20 kHz. The  $^7\text{Li}$  NMR signal in LiCl solution was used as a frequency reference  $\nu_0 = (\gamma/2\pi)H$  for the shift of NMR lines. The parameters of the electric field gradient (EFG) tensor,  $V_{ii}$ , quadrupole frequency,  $\nu_Q = (3eQ/2I(2I-1)\hbar)V_{ZZ}$ , and asymmetry parameter,  $\eta = (V_{XX} - V_{YY})/V_{ZZ}$  – were determined by computer simulation of the MAS NMR  $^7\text{Li}$  spectra [15].

#### 3. Calculation details

We used the local density approximation (LDA) and the tight-binding linear muffin-tin orbital (TB-LMTO) method [25] to generate the noninteracting band structure, which was used in the LDA+DMFT (cluster) calculations. The crystal structure was taken from Ref. 6. The calculations were performed on a dense mesh of 1728  $k$ -points in a full Brillouin zone. The Wannier function projection method [24] was employed to construct the low energy Hamiltonian for the Ru- $t_{2g}$  states.

As it was shown earlier, in the DFT calculations  $\text{Li}_2\text{RuO}_3$  is metallic in both low and high temperature phases [8], which contradicts to the experimental observation [6]. If we adopt Hubbard  $U$  correction in simplified methods such as LDA+ $U$ , we will stabilize solutions with electrons localized on the sites, not on the bonds and hence spoil molecular orbitals, which are obviously responsible for the formation of the spin-gap in  $\text{Li}_2\text{RuO}_3$ . Single site dynamical mean-field theory (DMFT) is also useless in this situation. Only the cluster extension of the LDA+DMFT calculation is able to treat the tendency to form the molecular orbital state and the strong Coulomb correlations (inherent to transition metals with unoccupied  $d$  shell) on equal footing.

The effective impurity model was solved by the Hirsh-Fye algorithm (HF-QMC) [23]. We chose typical values of the Hubbard repulsion parameter and Hund’s exchange for  $\text{Ru}^{4+}$ :  $U = 3\text{ eV}$  and  $J_H = 0.7\text{ eV}$  [26, 27]. The LDA+DMFT calculations were performed using the AMULET code. The uniform magnetic susceptibility was calculated as response to an external magnetic field.

$$\chi = \left. \frac{\delta m}{\delta h} \right|_{h \rightarrow 0} = \frac{n_\uparrow - n_\downarrow}{\delta E} \mu_B^2, \quad (1)$$

where  $\delta h$  is a small applied magnetic field,  $\delta E$  is corresponding Zeeman splitting (20 meV),  $\delta m(T)$  is a magnetization,  $n_\uparrow$  and  $n_\downarrow$  are the total occupation numbers for spin up and down.

We used nonmagnetic generalized gradient approximation [15] and linearized augmented plane wave method as realized in Wien2k package [16] to calculate electric field gradient tensor.